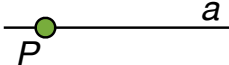
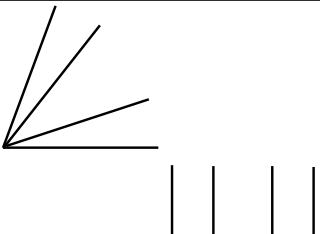
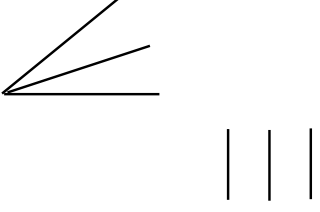
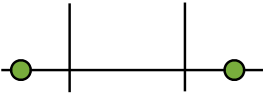

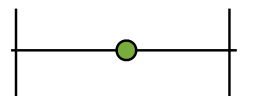
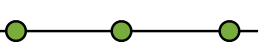
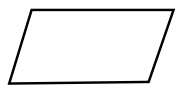


Geometry and Groups, a Dictionary

Geometric statements about points and lines	Picture in $R \times R$	Equivalent algebraic statements
point P lies on line a (or a passes through P)		$R_P \circ R_a = R_a \circ R_P$ $R_P \circ R_a$ is an involution
a is perpendicular to b	$a \perp b$	$R_a \circ R_b = R_b \circ R_a$ $R_a \circ R_b$ is an involution
a, b, c, d concurrent and $\angle(a, b) = \angle(d, c)$ OR no two of a, b, c, d intersect and $\text{dist}(a, b) = \text{dist}(d, c)$.		$R_a \circ R_b = R_d \circ R_c$
a, b, c are concurrent and the line b bisects $\angle(a, c)$ OR no two of a, b, c intersect and $\text{dist}(a, b) = \text{dist}(b, c)$.		$R_a \circ R_b = R_b \circ R_c$
b and d are \perp to PQ and $\text{dist}(P, b) = \text{dist}(d, Q)$		$R_P \circ R_b = R_d \circ R_Q$
b is the \perp bisector of PQ		$R_P \circ R_b = R_b \circ R_Q$
$b \parallel d$ and P is equidistant from the lines b and d		$b \neq d$ and $R_d \circ R_P = R_P \circ R_b$
M is the midpoint of AC		$R_A \circ R_M = R_M \circ R_C$
$AB = DC$ and $AB \parallel DC$		$R_A \circ R_B = R_D \circ R_C$

Bachmann's Axioms, Table from "*A New Look at Geometry*" by Irving Adler