

Lab Quiz 1.1

20 minutes

Name:

Student ID:

Always justify your answers!

Q1)... [2 points]

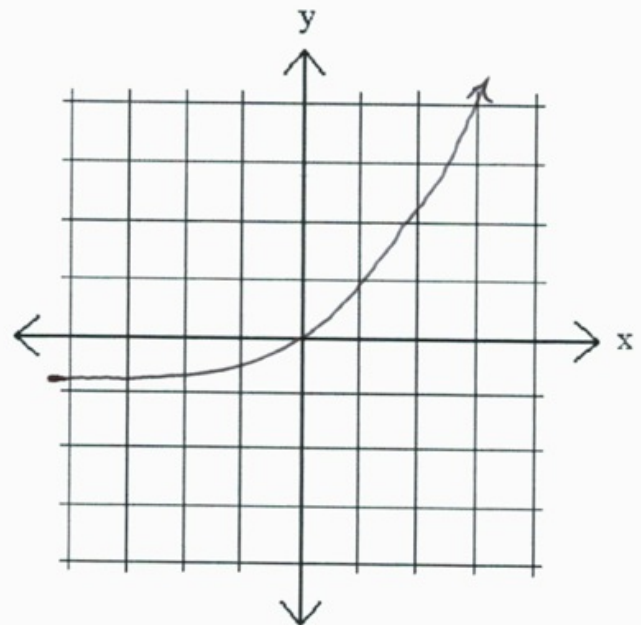
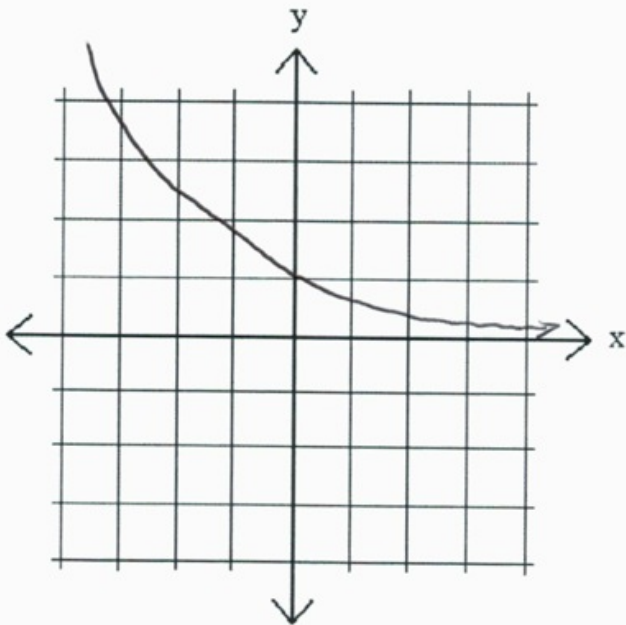
What is the domain of the function $f(x) = \sqrt{3x-5}$?

1pt for the $\longrightarrow 3x - 5 \geq 0$
inequality

1pt for rearranging
the inequality and
stating answer.

$$\left\{ \begin{array}{l} 3x \geq 5 \\ x \geq \frac{5}{3} \\ \text{or } x \text{ in } [5/3, \infty) \end{array} \right.$$

Q2)... [4 points] Roughly sketch the graph of each of these functions, clearly indicating any places where the function crosses the y axis: (a) $f(x) = e^{-x}$, (b) $g(x) = 2^x - 1$.



Each graph is 2pts, 1pt for correct y -intercept and
1pt for correct limits as $x \rightarrow \pm\infty$.

Q3]... [4 points] Decide whether or not the limit exists. If it exists, what is it?

(a) $\lim_{x \rightarrow 3} \frac{x+1}{x-3}$

$$\lim_{x \rightarrow 3^-} \frac{x+1}{x-3} = \frac{\text{positive}}{\text{negative}} = -\infty \quad] \quad 1 \text{ pt}$$

$$\lim_{x \rightarrow 3^+} \frac{x+1}{x-3} = \frac{\text{positive}}{\text{positive}} = +\infty \quad] \quad 1 \text{ pt}$$

Since left and right limits are different, the limit does not exist.

(b) $\lim_{x \rightarrow -3} \frac{x^2+x-6}{x+3}$

$$x^2 + x - 6 = (x+3)(x-2) \quad] \quad 1 \text{ pt for factoring}$$

$$\text{so } \lim_{x \rightarrow -3} \frac{(x+3)(x-2)}{(x+3)} = \lim_{x \rightarrow -3} x-2 = -3-2 = -5$$

1pt for canceling and taking limits.